

# DE-FEM: A NEW ENRICHED FORMULATION FOR MODELING WEAK AND STRONG DISCONTINUITIES

Alejandro M. Aragón<sup>1,\*</sup>, Jian Zhang<sup>1</sup>, Sanne J. van den Boom<sup>1</sup>, Elena De Lazzari<sup>1</sup>, Dongyu Liu<sup>2</sup>, Max van der Kolk<sup>1</sup>, Matthijs Langelaar<sup>1</sup>, Angelo Simone<sup>2,3</sup>, and Fred van Keulen<sup>1</sup>

<sup>1</sup> Faculty of Mechanical, Maritime and Materials Engineering  
Delft University of Technology, Delft, the Netherlands

<sup>2</sup> Faculty of Civil Engineering and Geosciences  
Delft University of Technology, Delft, the Netherlands

<sup>3</sup> Department of Industrial Engineering University of Padua, Padova, Italy

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Weak and strong discontinuities play an important role in the analysis of a wide range of problems, such as fracture or multi-phase materials. In standard Finite Element Analysis (FEA), discontinuities are explicitly taken into account by ensuring that any material interfaces, domain boundaries, and/or cracks coincide with element sides. Because creating such a matching mesh can be a challenging exercise, especially when dealing with moving discontinuities, enriched formulations such as the eXtended/Generalized Finite Element Method (X/GFEM) have recently gained considerable visibility. X/GFEM treats discontinuities in an elegant manner by decoupling them from the discretization. Yet, many properties of standard FEA that were taken for granted are lost in X/GFEM.

The Discontinuity-Enriched Finite Element Method (DE-FEM) [1] was recently introduced as a novel enriched formulation to model weak and strong discontinuities with a unified formulation. DE-FEM recovers the appealing properties of standard FEA, while keeping the mesh-discontinuity decoupling feature offered by X/GFEM.

In this presentation, we will demonstrate the versatility of DE-FEM in the context of fracture mechanics, granular materials, immersed domains, and fluid-structure interaction. We illustrate the method for modeling 2-D and 3-D cracks, and NURBS-enhanced discontinuities. Furthermore, we demonstrate DE-FEM as an immersed boundary (or embedded domain) method for problems in elasticity and in the context of fluid dynamics and fluid-structure interaction. Finally, we show the stability of the method with regards to the condition number of the resulting system matrices.

## REFERENCES

- [1] A. M. Aragón and A. Simone, The Discontinuity-Enriched Finite Element Method. *Int. J. Numer. Meth. Eng.*, Vol. **112** (11), pp. 1589–1613, 2017.