

MICROSTRUCTURAL MODELS OF LIGAMENT AND TENDON ELASTICITY AND VISCOELASTICITY

Tom Shearer^{1,2,*}, William J. Parnell¹, Barbara Lynch³, Hazel R.C. Screen⁴, I. David Abrahams⁵ and Chavaunne T. Thorpe⁶

¹ School of Mathematics, University of Manchester M13 9PL, UK

² School of Materials, University of Manchester M13 9PL, UK

³ Solids Mechanics Laboratory, Ecole Polytechnique, Centre National de la Recherche Scientifique, Institut National de la Santé et de la Recherche Medicale U696, Palaiseau Cedex, France

⁴ Institute of Bioengineering and Materials Science, Queen Mary University of London, Mile End Road, London E1 4NS

⁵ Isaac Newton Institute, University of Cambridge, Clarkson Road, Cambridge CB3 0EH, UK

⁶ Department of Comparative Biomedical Sciences, The Royal Veterinary College, Royal College Street, London NW1 0TU, UK

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Ligaments and tendons are vital connective structures in the musculoskeletal systems of vertebrates that consist of collagen fibres organised in a hierarchical structure. Their main subunit is the fascicle which is made of crimped fibrils. In this talk, I will discuss two models that describe the mechanical behaviour of ligaments and tendons and are based on the microstructure mentioned above.

The first model is a non-linear elastic model, which is expected to be valid in the low strain-rate limit. I will present a strain energy function for modelling ligaments and tendons based on the geometrical arrangement of their fibrils [1], and will compare the ability of the new model to reproduce experimental data with that of the commonly-used Holzapfel-Gasser-Ogden model [2]. I will then use the new model to explain the mechanical differences between positional and energy-storing tendons [3].

The second model is a viscoelastic model. By assuming that each fibril is now linearly *viscoelastic*, I will show that several complex, non-linear viscoelastic effects arise directly as a result of there being a *distribution* of fibril crimp lengths. The viscoelastic model accurately predicts the results of cyclic tensile tests, and can reproduce different data sets with a single set of constitutive parameters simply by changing the crimp distribution parameters.

REFERENCES

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