

## Error Estimation for Isogeometric Analysis of the Stokes and Navier-Stokes equations

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**Key Words:** *Isogeometric analysis, error estimation, adaptive refinement, Navier-Stokes equation.*

In this article, we will develop and present suitable error estimators for adaptive mixed isogeometric methods for solving the Stokes and Navier-Stokes equations. We will compare the use of residual-based error estimators with superconvergent patch recovery methods [1]. The adaptive refinement will be based on the use of LR B-splines [2], and the recently proposed methods using isogeometric Taylor-Hood, Sub-grid Taylor-Hood [3], and divergence-conforming elements [4]. The different estimators will be thoroughly tested on problems with (manufactured) analytical solutions.

### REFERENCES

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