

# FAST SPECTRAL SOLVERS WITHOUT LINEAR REFERENCE MEDIUM

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In the field of computational homogenization of periodic representative volume elements (RVE), over the last two decades, fast Fourier transform (FFT)-based spectral solvers have emerged as a promising alternative to the finite element method (FE). Most of these spectral methods are based on the work of Moulinec and Suquet [1] and split an RVE’s mechanical response into the response of a linear reference medium and a periodic fluctuation due to heterogeneities. The main advantage of this formulation over FE is that it can be both significantly faster and have a much smaller memory-footprint. The two main problems are 1) the choice of the linear reference medium, which is typically based on heuristics, is not trivial and has a strong impact on the method’s convergence (A bad choice can render the method non-convergent), and 2) convergence is not necessarily uniformly. Numerous studies have suggested mitigations to both of these problems (e.g. [2]), but they have remained substantial disadvantages compared to the more expensive, but also more robust FE.

Recent work by Zeman et al. [3] proposes a new formulation for spectral solvers which dispenses with the linear reference problem and converges unconditionally. We present  $\mu$ Spectre, an open HPC implementation of this novel method and use it to show that the new approach is much more computationally efficient than its linear reference medium-based predecessors, converges in the presence of arbitrary phase contrast - including porosity - without Gibbs ringing artifacts.

## REFERENCES

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