

Spectral Galerkin Method for Solving Helmholtz and Laplace Dirichlet Problems on Multiple Open Arcs

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We present a spectral numerical scheme for solving Helmholtz and Laplace problems with Dirichlet boundary conditions on an unbounded non-Lipschitz domain $\mathbb{R}^2 \setminus \bar{\Gamma}$, where Γ is a finite collection of open arcs. An indirect method is employed, giving rise to first kind formulations whose variational forms are discretized using weighted Chebyshev polynomials. Well-posedness of the continuous and discrete problems is established as well as spectral convergence under the existence of analytic maps to describe the arcs. In order to reduce computation times, a simple matrix compression technique based on sparse approximations of the kernel is developed. Numerical results are provided to validate our claims pointing out to new improvements and extensions.

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