

NUMERICALLY EFFICIENT IMPLEMENTATION OF RATE-INDEPENDENT GRADIENT ENHANCED CRYSTAL PLASTICITY

Volker Fohrmeister^{1,*} and Jörn Mosler¹

¹ TU Dortmund University, Institute of Mechanics, Leonhard-Euler-Str. 5, D-44227 Dortmund, e-mail: {volker.fohrmeister, joern.mosler}@tu-dortmund.de, www.iofm.de

Keywords: *Gradient Enhanced Elastoplasticity, Crystal Plasticity, Numerical Efficiency*

A convenient and natural way to incorporate size effects – like the well-known Hall-Petch relation – into crystal plasticity theory is to account for gradients of the internal variables. A novel numerically efficient algorithmic formulation for these gradient-enhanced crystal plasticity models is presented. This formulation also covers (standard) local crystal plasticity theory, cf. [1]. Two main problems encountered in numerical implementations of such crystal plasticity theories are: (a) determination of the active slip systems and (b) ill-posedness of the discretized constitutive model, if too many slip systems are simultaneously active, cf. [2]. An efficient formulation for solving such problems is presented in [3]. This formulation relies on the introduction of (i) nonlinear complementary functions in order to eliminate the inequalities characterizing rate-independent plasticity theory and (ii) a purely numerical viscous relaxation by means of an augmented Lagrangian. In this talk, the algorithmic formulation proposed in [3] is critically analyzed and significantly extended for gradient-enhanced crystal plasticity theory. Furthermore the resulting formulation is embedded into the framework of incremental energy minimization.

REFERENCES

- [1] J. R. Rice, Inelastic constitutive relations for solids: an internal variable theory and its application to metal plasticity. *Journal of the Mechanics and Physics of Solids*, Vol. **15**, pp. 1197–1215, 1971.
- [2] J. Schröder and C. Miehe, Aspects of computational rate-independent crystal plasticity, *Computational Materials Science*, Vol. **9**, pp. 168–176, 1997.
- [3] M. Schmidt-Baldassari, Numerical concepts for rate-independent single crystal plasticity. *Computer Methods in Applied Mechanics and Engineering*, Vol. **192**, pp. 1261–1280, 2003.
- [4] M. Ekh, M. Grymer, K. Runesson and T. Svedberg, Gradient crystal plasticity as part of the computational modelling of polycrystals. *International Journal for Numerical Methods in Engineering*, Vol. **72**, pp. 197–220, 2007.